In this paper, we consider some classes of Brownian functionals, including non-smooth functionals (therefore, it is impossible to use the well-known Clark-Ocone formula), depending both on the trajectory and on the last moment of time, and propose a new method for obtaining a constructive stochastic integral representation in the case of both smooth and non-smooth functionals.